# Epistemic Disjunction and Obligatory Ignorance

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### Outline

- Puzzle: how some disjunctions in Russian are special
- Background: exhaustification, exclusivity, free choice and distributive inferences
- Proposal: obligatory ignorance and its representation
- Summing up: what has been learned

#### 1. Puzzle

- There are two complex disjunctions in Russian, *to li...to li...* and *ne to...ne to...*, with special properties that set them apart both complex disjunctions (*ili...ili...* in Russian, *soit...soit...* in French) and from simple disjunctions (*ili* in Russian, *or* in English, *ou* in French etc.).
- Ignorance and exclusivity inferences

*To li...to li...* and *ne to...ne to...* pattern with other disjunctions:

- (1) a. John saw (either) a cat <u>or</u> a dog.
  - b. Jean a vu un chat <u>ou</u> un chien.
  - c. Džon videl košku <u>ili</u> sobaku.
- (2) a. Jean a vu soit un chat soit un chien.
  - b. Džon videl <u>ili</u> košku, <u>ili</u> sobaku. *John saw or a cat or a dog*
- (3) Džon videl to li košku, to li sobaku / ne to košku, ne to sobaku.
- (1), (2), (3)

 $\rightarrow \neg B_S[John saw a cat] \& \neg B_S[John saw a dog]$ 

*Ignorance* 

 $\hookrightarrow$  B<sub>S</sub>[¬ [John saw both a cat and a dog]]

**Exclusivity** 

- Scope of disjunction w.r.t. to negation

Simple disjunctions are local PPIs in Russian and French (Spector 2014), but not in English:

(4) a. John didn't see (either) a cat <u>or</u> a dog.

b. Jean n'a pas vu un chat <u>ou</u> un chien.

c. Džon ne videl košku <u>ili</u> sobaku.

Wide scope w.r.t. negation:  $\neg$  [John saw a cat]  $\lor \neg$  [John saw a dog]]  $\lor (4a) \lor (4b) \lor (4c)$ 

<sup>\*</sup> Many thanks to Sam Alxatib, Danny Fox, Sasha Podobryaev, and the anonymous reviewers for helpful comments.

- (5) a. John doubts that he saw a cat <u>or</u> a dog.
  - b. Jean doute qu' il ait vu un chat ou un chien.
  - c. Džon somnevaetsja čto pro videl košku <u>ili</u> sobaku

Narrow scope w.r.t. negation: J. doubts [J. saw a cat v J. saw a dog] (5a) (5b) (5c) Wide scope w.r.t. negation: J. doubts [J. saw a cat] v J. doubts [J. saw a dog] (5a) (5b) (5c)

Complex disjunctions are global PPIs in both French (Spector 2014) and Russian:

- (6) a. Jean n'a pas vu <u>soit</u> un chat <u>soit</u> un chien. \*  $\neg > \lor$ ;  $\checkmark \lor > \neg$  b. Džon ne videl <u>ili</u> košku <u>ili</u> sobaku. \*  $\neg > \lor$ ;  $\checkmark \lor > \neg$  *John didn't see or a cat or a dog*
- ait vu soit un chat soit un chien. (7)a. Jean doute qu' il \* ¬ > V; \(^\dagger V > ¬ \* ¬ > V: V > b. Džon somnevaetsja čto *pro* videl ili košku ili sobaku. John doubts that he saw a cat a dog

*To li...to li...* and *ne to...ne to...* pattern with French and Russian complex disjunctions:

- (8) Džon ne videl <u>to li</u> košku, <u>to li</u> sobaku. \*  $\neg > \lor$ ;  $\checkmark \lor > \neg$  *John didn't see TO LI a cat TO LI a dog*
- (9) Džon somnevaetsja čto pro videl <u>to li</u> košku, <u>to li</u> sobaku. \* ¬ > V;  $\checkmark$  V > ¬ John doubts that he saw TOLI a cat TOLI a dog
  - Free choice and distributive inferences

Under existential modals, disjunctions normally give rise to free choice permission inferences, in which case ignorance is obviated. This is true for all simple and complex disjunctions in English, French and Russian (10), except for to li...to li.../ne to...ne to... (11):

- (10) a. You may take (either) an apple  $\underline{\text{or}}$  an orange.
  - b. Tu peut prendre une pomme <u>ou</u> une orange.
  - c. Ty možeš vzjať jabloko <u>ili</u> apeľsin.
- $\hookrightarrow$  You may take an apple & You make take an orange Free Choice
- (11) a. Tu peut prendre <u>soit</u> une pomme <u>soit</u> une orange. b. Ty možeš vzjat' <u>ili</u> jabloko, <u>ili</u> apel'sin. You may take or an apple or an orange
- (12) Ty možeš vzjať <u>to li</u> jabloko, <u>to li</u> apeľsin / ne to jabloko, ne to apeľsin *You may take TO LI an apple TO LI an orange*
- $\checkmark$  You may take an apple & You make take an orange \*Free Choice (  $\hookrightarrow$  It is either an apple or an orange (I am not sure) that you are allowed to take. )

Under universal quantifiers, disjunctions give rise to distributive inferences (see Crnič et al. 2015 for a recent discussion). In these cases ignorance can be obviated. Again, this is true for for all simple and complex disjunctions in English, French and Russian (13a,b,c), but not for *to li...to li.../ne to...ne to...* (13d):

- (13) <u>Scenario:</u> Three boys arrived: John, Bob, and Bill. I see that Bill brought a dog, Bob also brought a dog, and John brought a cat. I have no doubts about which boy brought which pet.
  - a. Every boy brought (either) a cat <u>or</u> a dog.
  - b. Chaque garçon a apporté un chat <u>ou</u> un chien / <u>soit</u> un chat, <u>soit</u> un chien.
  - c. Každyj mal'čik prinës (ili) košku <u>ili</u> sobaku.
  - d. \* Každyj mal'čik prinës <u>to li</u> košku <u>to li</u> sobaku / <u>ne to</u> košku, <u>ne to</u> sobaku. Every boy brought TO LI a cat TO LI a dog

### 2. Background

I adopt a grammatical view of scalar implicatures that disjunctions give rise to.

- Scalar implicatures are brought about by a covert exhaustification operator EXH (cf. Fox 2007, Chierchia et al. 2012 building on proposals in Groenendijk and Stokhof 1984, Krifka 1995, Landman 1998, and van Rooy 2002)
- (14) EXH<sub>ALT</sub>(p)(w)  $\Leftrightarrow p(w) \& \forall q$ :  $q \in \text{EXCL}_{\text{ALT}}$ .  $\neg q(w)$ , where EXCL<sub>ALT</sub> is a subset of ALT containing all and only *innocently excludable alternatives* (see Fox 2007 for a strict definition)
  - Exclusivity inferences in unembedded environments are derived straightforwardly:
- (15)  $EXH_{ALT}[P(x)\vee Q(x)] \Leftrightarrow [P(x)\vee Q(x)] \& \neg [P(x)\&Q(x)]$ 
  - Distributive inferences with disjunctions arise when EXH takes scope over a universal quantifier:
- (16)  $\text{EXH}_{\text{ALT}} \left[ \forall x \left[ P(x) \vee Q(x) \right] \right] \Leftrightarrow \forall x \left[ P(x) \vee Q(x) \right] \& \neg \forall x \left[ P(x) \right] \& \neg \forall x \left[ Q(x) \right]$ 
  - Free choice permission inferences are brought about by double exhaustification above the existential modal:
- (17) a. LF:  $EXH_{ALT_2}[EXH_{ALT_1}[\lozenge[PvQ]]]$ 
  - b. Alt1 = {  $\langle PvQ \rangle$ ,  $\langle P, \langle Q, \langle P&Q \rangle$  }  $\begin{aligned}
    & \text{EXH}_{ALT1}[\langle PvQ \rangle] \Leftrightarrow \langle PvQ \rangle & \neg \langle P&Q \rangle \\
    & \text{Alt2} = { \text{EXH}_{ALT1}[\langle P \rangle], \text{EXH}_{ALT1}[\langle Q \rangle] } = { \langle P& \neg \langle Q, \langle Q& \neg \langle P \rangle \rangle } \end{aligned}$
  - c.  $\text{EXH}_{\text{ALT}_2}\left[\text{EXH}_{\text{ALT}_1}\left[\lozenge[\text{PvQ}]\right]\right] \Leftrightarrow \lozenge[\text{PvQ}] \& \neg \lozenge[\text{P&Q}] \& \neg[\lozenge{\text{P}} \& \neg \lozenge{\text{Q}}] \& \neg[\lozenge{\text{Q}} \& \neg \lozenge{\text{P}}] \Leftrightarrow \lozenge[\text{PvQ}] \& \neg \lozenge[\text{P&Q}] \& [\neg \lozenge{\text{P}} \text{ v} \lozenge{\text{Q}}] \& [\neg \lozenge{\text{Q}} \text{ v} \lozenge{\text{P}}] \Leftrightarrow \lozenge{\text{P}} \& \lozenge{\text{Q}}$

#### 3. Proposal

Recall that *to li...to li...* and *ne to...ne to...* have some special properties. Let's focus on the following two:

- They do not give rise to Free Choice inferences and ignorance obviation under existential modals.
- They also do not lead to ignorance obviation under universal quantifiers.

Both properties would follow if ignorance inferences associated with *to li...to li...* and *ne to...ne to...* are made obligatory.

Here is a way to formalize this intuition:

- (18) Disjunctions *to li...to li...* and *ne to...ne to...* have to appear in the *immediate scope* of some doxastic/epistemic necessity operator, by default, Meyer's (2013) K-operator.
  - According to Meyer 2013, every utterance is embedded under K, and ignorance inferences are computed in the grammar via exhaustification above K:
- (19) EXH  $[K(P \lor Q)] \Leftrightarrow K[P \lor Q] \& \neg K(P) \& \neg K(Q) \& \neg K(P \& Q)$

If to li...to li... and ne to...ne to... have to appear in the immediate scope of K, obligatory ignorance would follow.

- No Free Choice inferences and ignorance obviation under existential modals: Given (18) and the assumption that EXH K must take the highest scope, *to li...to li.../ne to...ne to...* should scope above the existential modal, which would exclude Free Choice and lead to ignorance.
- No ignorance obviation under universal quantifiers: trivially, given (18).

Interestingly, universal quantifiers seem to be able to scope above  $EXH\ K^1$ . When they do, we get cases of *distributed ignorance*.

- (20)  $\forall x \left[ \text{EXH} \left[ K \left[ P(x) \vee Q(x) \right] \right] \right] \Leftrightarrow \forall x \left[ K \left[ P(x) \vee Q(x) \right] \& \neg K \left[ P(x) \right] \& \neg K \left[ Q(x) \right] \right]$
- (21) <u>Scenario:</u> I am watching a gathering of three boys in the street from my apartment on the 12<sup>th</sup> floor. I am sure that each of them brought some pet, in each case it looks like either a cat or a dog, but it is hard to see who brought what exactly.

Každyj mal'čik prinës <u>to li</u> košku, <u>to li</u> sobaku / <u>ne to</u> košku, <u>ne to</u> sobaku. Every boy brought TO LI a cat TO LI a dog

When to li...to li... and ne to...ne to... appear in the immediate scope of a universal attitude that is different from Meyer's K, ignorance is obligatorily attributed to the attitude holder, so, a sentence like (22) are ambiguous with respect to its ignorance inferences.

<sup>&</sup>lt;sup>1</sup> Note possible connections to Krifka's (2001) proposal that universal quantifiers can quantify into speech acts.

(22) Bob polagaet, čto Bill prinës to li košku to li sobaku.

Bob believes that Bill brought TO LI a cat TO LI a dog

→ ¬K[BELIEVE<sub>Bob</sub> [Bill brought a dog]] & ¬K[BELIEVE<sub>Bob</sub> [Bill brought a dog]]

- Speaker's Ignorance

Or: → K[¬BELIEVE<sub>Bob</sub> [Bill brought a dog]]

- Attitude Holder's Ignorance

A prediction: no relativized ignorance under existential attitudes:

(23) Bob dopuskaet, čto Bill prinës to li košku to li sobaku.

Bob considers.it.possible that Bill brought TO LI a cat TO LI a dog

→ ¬K[C.I.P.Bob [Bill brought a dog]] & ¬K[BELIEVEBob [Bill brought a dog]]

- Speaker's Ignorance

But 

K[¬BELIEVEBob [Bill brought a dog]] & ¬BELIEVEBob [Bill brought a dog]]

- \*Attitude Holder's Ignorance

## 4. Summing up

- Some complex disjunctions (specifically, *to li...to li...* and *ne to...ne to...* in Russian) give rise to obligatory, non-cancellable ignorance inferences. This property sets them apart from other known complex and simple disjunctions<sup>2</sup>.
- A way to capture this property is to stipulate that they have to appear in the *immediate scope* of some doxastic/epistemic necessity operator, by default, Meyer's (2013) K-operator. Ignorance inferences arise as a result of exhaustification immediately above the operator.

It would be worth exploring the parallels with the behavior of epistemic indefinites (cf. Aloni and Port 2011, Aloni 2012, Alonso-Ovalle and Menéndez-Benito 2003, Fălăuş 2014, Kratzer and Shimoyama 2002, among many others), especially the Russian –to series (see Haspelmath 1997, Yanovich 2005), which seems to have a very similar semantic distribution.

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<sup>&</sup>lt;sup>2</sup> The PPI property that is shared by all complex disjunctions including *to li...to li...* and *ne to...ne to...* (see examples (6–9) remains mysterious. While my proposal may be able to explain it for *to li...to li...* and *ne to...ne to...* (given (18)), it cannot be extended to other complex disjunctions. At the same time, the only idea I am aware of, that is, Spector's (2014) proposal that complex disjunctions are special in that they have to be in the scope of EXH, is not quite compatible with Meyer's 2013 claim, which I build upon, that EXH is present in sentences with simple disjunctions as well.

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