# The best response: Speaker rationality in an interactive paradigm 

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## Section 1

## Implicature in Complex Sentences

## Scalar Implicature and Implicature of Complex Sentences

Example (Unembedded implicature trigger)

1. Some of the girls found marbles.
$+>$ Not all found marbles.

Example (Embedded implicature trigger)

1. Every girl found some of their marbles.

## The Standard Theory

Levinson (1983)

Example (Unembedded implicature trigger)
Some of the girls found marbles. $=A($ some $)$
$+>$ Not all girls found marbles.

## Reasoning:

- $A($ all $)$ : would have been more informative
- Speaker did't say $A(a l l)$ but $A($ some $)$
- Hence, he must believe $\neg A$ (some)
- Cooperativity + competence $\Rightarrow \neg A$ (some)

Horn scales: $\langle$ all, some $\rangle,\langle a n d$, or $\rangle, \ldots$

## Embedded Implicature

## Example

1. Every girl found some of her marbles.
2. Some of the girls found some of their marbles.

## Variously predicted readings:

(Chierchia 2004, Sauerland 2004, Chierchia et al 20012)

1. Every girl found some of her marbles.

- literal: Every girl found some and possibly all of her marbles.
- global: Not every girl found all of her marbles.
- local: Every girl found some but not all of her marbles.

2. Some of the girls found some of their marbles.

- glob/loc: Not all of the girls found some of their marbles.
- glob: None of the girls found all of her marbles.


## Game Theory and Complex Sentences

Interactional approaches:

- Franke (2009) / Jäger (2013): Iterated Best Response Models.
- Benz (2012): Error Models.
- Pavan (2013) / Rothschild (2013): Iterated Admissibility Models.
- Bergen et al. (in print), Potts et al. (in print): Bayesian Models.


## Problem:

- GT provides no technique for analysing linguistic structure.
- Seems to be confined to a globalist approach.


## Aims of this Talk

- Present a specific model of implicature in complex sentences.
- Introduce new interactive experimental paradigm for testing the model.
- Evaluate experimental results/different speaker strategies.


## Section 2

## Error Models

## Error Models

## Benz 2012

- Communication as stochastic process (Shannon 1948).



## Error Models

## Benz 2012

- Communication as stochastic process (Shannon 1948).


Implicature

- If hearer can uniquely recover intended message $\Rightarrow$ Success.
- If not $\Rightarrow$ Clarification request.


## Error Models: Critical Example

## The Role of Errors

## Example (Bus Ticket)

An email was sent to all employees that bus tickets for a joint excursion have been bought and are ready to be picked up. By mistake, no contact person was named. Hence, $H$ asks one of the secretaries:
$H$ : Where can I get the bus tickets for the excursion?
$S$ : Ms. Müller is sitting in office 2.07. ( $U_{M 2.07}$ )
$+>$ Bus tickets are available from Ms. Müller.

## Problem:

- Hearer finds list with all room numbers of all employees. $\nRightarrow$ Goes to 2.07.
$\Rightarrow$ Literal content not enough for inducing hearer to choose intended action.


## A Game Tree



- Problem: $E U\left(\right.$ go-2.07 $\left.\mid \llbracket U_{M 2.07} \rrbracket\right)=E U\left(\operatorname{search} \mid \llbracket U_{M 2.07} \rrbracket\right)=\varepsilon$.
- Implies: Literal content is irrelevant.


## How it should have been played



- Literal content is deciding optimal action.
- In Example speaker omitted part of message.


## Omitting Part of Message



- Literal content is deciding optimal action.
- In Example speaker omitted part of message.


## Presentation in Table

- Consider for each state of affairs the optimal assertions.
- Consider all utterances which can result from omitting a conjunct of message.
$\Rightarrow$ Noise ( $\mathscr{N}_{\varphi}$ )
- Consider the reduced utterances from which the original message can be reconstructed. $\left(\mathscr{U}_{\varphi}\right)$

| $\varphi$ | $\operatorname{Lit}(\varphi)$ | $\mathscr{N}_{\varphi}$ | $\mathscr{U}_{\varphi}$ |
| ---: | :--- | :--- | :--- |
| $\varphi_{\text {Mhas } / 2.07}$ | $U_{M \text { has } / 2.07}$ | $U_{M \text { has } / 2.07}, F_{M \text { has }}, U_{M 2.07}$ | $U_{M 2.07}$ |
| $\varphi_{\text {Mhas } / 3.11}$ | $F_{M \text { has } / 3.11}$ | $F_{M \text { has } / 3.11}, F_{M \text { has }}, F_{M 3.11}$ | $F_{M 3.11}$ |
| $\varphi_{\text {Shas } / 2.07}$ | $F_{S \text { has } / 3.11}$ | $F_{S_{\text {has } / 3.11}}, F_{S \text { has }}, F_{S 3.11}$ | $F_{S 3.11}$ |
| $\varphi_{\text {Shas } / 3.11}$ | $U_{S \text { has } / 3.11}$ | $U_{S \text { has } / 3.11}, F_{S \text { has }}, F_{S 3.11}$ | $F_{S 3.11}$ |

## Characteristics

- Uniform explanation of relevance and quantity implicature
- No gambling: short utterances communicate message with certainty
- No blocking: preference for short utterances does not lead to risky utterances
- No hidden semantic operators


## Section 3

## Testing for Implicature by Decision Making

The basic best response paradigm Nicole Gotzner \& Anton Benz

## Scenario

## Background:

- 4 girls who each own a set of 4 special edition marbles (Degen \& Goodman, 2014);
- marbles get lost during play and girls have to find them
- mother offers rewards to girls

Reward system:

- chocolate: girl finds all 4 of her marbles
- candy: girl finds fewer than 4 of her marbles
- gummy bears: girl finds none of her marbles (consolation prize)


## Instructions

- Mother tells participants how many marbles each girl found
- Task: Participants are asked to buy sweets for the girls


## Example

Sentence: No girl found any of her marbles

| Chocolate | $\square$ | YES | $X$ | No |
| :--- | :--- | :--- | :--- | :--- |
| Candy | $\square$ | YES | $X$ | No |
| Gummy bear | $X$ | YES | $\square$ | No |

## The Experiment as Signalling Game

## Playing the game:

1. Mother = speaker knows actual world
2. Mother chooses an utterance
3. Subject chooses an action: buying sweets
4. Game ends

- Game structure common knowledge
- Game of pure coordination: preferences aligned


## Preferences:

- Every girl should get her appropriate sweet
- No superfluous sweets should be bought


## Seven possible worlds

- $\exists \mid \nexists$ : Some found none
- $\exists \mid \exists^{\prime}$ : Some found some but not all
- $\exists \mid \forall$ : Some found all

| $\exists \exists \mid \nexists$ | $\exists \mid \exists!$ | $\exists \mid \forall$ | world |
| :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | $v_{1}=\square_{1}$ |
| 0 | 1 | 0 | $v_{2}=\square_{2}$ |
| 0 | 0 | 1 | $v_{3}=\square_{3}$ |
| 1 | 1 | 0 | $v_{4}=\square_{4}$ |
| 1 | 0 | 1 | $v_{5}=\square_{5}$ |
| 0 | 1 | 1 | $v_{6}=\square_{6}$ |
| 1 | 1 | 1 | $v_{7}=\square_{7}$ |

## Seven possible actions

## Actions

- I: Gummy bear
- I: Candy
- I: Chocolate


## Best responses

| world | act | world | act | world | act |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $v_{1}=\square_{1}$ | -- | $v_{4}=\square_{4}$ | II. | $v_{7}=\square_{7}$ | IIII |
| $v_{2}=\square_{2}$ | -- | $v_{5}=\square_{5}$ | -. |  |  |
| $v_{3}=\square_{3}$ | _-\ | $v_{6}=\square_{6}$ | _\|I |  |  |

## Effect of Uncertainty

## Best responses



- In all other cases: ||||


## Error Models for Complex Sentences

## Different alternatives:

- Alternative utterances constructed from worlds.

Literal descriptions of worlds:

| world | utterances | world | utterances |
| :---: | :---: | :---: | :---: |
| $\square 1$ | $U_{\forall \mid \exists}$ | $\square_{4}$ | $U_{\exists!\mid \exists} \wedge U_{\exists!\mid \exists!} \wedge U_{7 \backslash \mid \forall}$ |
|  | $\cup_{7 \text { 7] }}$ | $\square_{5}$ | $U_{\exists!\mid \nexists} \wedge U_{\exists \exists \mid \exists!} \wedge U_{\exists!\mid \forall}$ |
| $\square 2$ | $U_{\forall \mid \exists!}$ | ${ }_{6}$ | $U_{\forall \mid \exists} \wedge U_{\exists!\mid \forall} \wedge U_{\text {ق! } \mid \exists!}$ |
|  | $U_{\forall \mid \exists} \wedge U_{\text {㓞 }}$ |  | $U_{\exists!\mid \forall} \wedge U_{\exists!\mid \exists!} \wedge U_{\exists \exists \mid \exists \exists}$ |
| ${ }^{3}$ | $U_{\forall \mid V}$ | $\square_{7}$ | $U_{\exists!\mid \forall} \wedge U_{\exists!!\exists!} \wedge U_{\exists!!\exists}$ |

- $U_{Q \mid Q^{\prime}}: Q$ of the girls found $Q^{\prime}$ of the marbles.
- $\exists$ !: some but not all, $\nexists$ : none


## Error Models for Complex Sentences

- Shorter utterances constructed by elimination rules


## Elimination rules:

1. $U_{(\exists!)} \rightarrow U_{(\exists)}$ : reduction of 'some but not alf to 'some'
2. $U_{\exists \mid \alpha} \wedge U_{\beta} \rightarrow U_{\beta}$ : elimination of conjuncts with empty subjects

## Restrictions:

- Rule $U_{x} \rightarrow U_{y}$ only applicable if $\llbracket U_{x} \rrbracket \subseteq \llbracket U_{y} \rrbracket$
- Requirement: unique recoverability of meaning (long story)


## Application of Elimination rules

## Literal descriptions of worlds：

－world utterances

| －1 | $U_{\forall \mid \exists \wedge} \wedge U_{7\|\exists\|} \wedge U_{7 \mid \forall}$ |
| :---: | :---: |
| $\square 2$ | $U_{\nexists \mid \exists \exists} \wedge U_{\forall \mid \exists!} \wedge U_{\exists \exists \mid \forall}$ |
| ${ }^{3}$ | $U_{\nexists\|\exists\| 7} \wedge U_{\text {羽 }!} \wedge U_{\forall \mid \forall}$ |
| $\square_{4}$ | $U_{\exists!\mid \exists \wedge} \wedge U_{\exists!\mid \exists!} \wedge U_{\exists \exists \mid \forall}$ |


| world | utterances |
| :---: | :---: |
| $\square_{5}$ |  |
| $\\|_{6}$ | $U_{\exists \exists \mid \exists \exists} \wedge U_{\exists!\| \|!} \wedge U_{\exists ⿰ 习 习}^{1 \mid \forall}$ |
| 17 | $U_{\exists!\mid \nexists} \wedge U_{\exists!\mid \exists!} \wedge U_{\exists!\mid \forall}$ |

## Application of Elimination rules

## Elimination of 'none of the girls ...:

- world utterances




## Application of Elimination rules

## Elimination of some but not all:

- world utterances

| $\square_{1}$ | $U_{\forall \mid \exists \exists}$ |
| :--- | :--- |
| $\square_{2}$ | $U_{\forall \mid \exists}$ |
| $\square_{3}$ | $U_{\forall \mid \forall}$ |
| $\square_{4}$ | $U_{\exists \mid \exists} \wedge U_{\exists \mid \exists}$ |


| world | utterances |
| :---: | :--- |
| $\square U_{7}$ | $U_{\exists \exists \nexists} \wedge U_{\exists \mid \forall}$ |
| $\square U_{6}$ | $U_{\exists \exists \exists} \wedge U_{\exists \mid \forall}$ |
| $\square \coprod_{7}$ | $U_{\exists \mid \exists} \wedge U_{\exists \mid \exists} \wedge U_{\exists \mid \forall}$ |

## Application of Elimination rules

## Predicted maximal simplification:

- world utterances

| $\square_{1}$ | $U_{\forall \mid \exists}$ |
| :--- | :--- |
| $\square_{2}$ | $U_{\forall \mid \exists}$ |
| $\square_{3}$ | $U_{\forall \mid \forall}$ |
| $\square_{4}$ | $U_{\exists \mid \exists} \wedge U_{\exists \mid \exists}$ |

## Testing the Model

## Testable predictions:

- utterance length increases with complexity of world.
- critical strategy not less efficient than average human strategy.
- strategy is efficient:
- increasing average utterance length does not increase communicative success.
- decreasing average length should decrease communicative success (??) (claim in general probably not correct, however, we expected it in marble scenario)


## Section 4

## The interactive best response paradigm

Anton Benz \& Nicole Gotzner

## The interactive best response paradigm

- Participants play best response paradigm in groups, taking two different roles (speaker and hearer)
- Speaker's task: Describe state of the world represented by picture
- Response options: all, some, none, some but not all, some and possibly all, any (up to 5 sentences)

Lisa

Susi
Einige
der Mädchen fand(en) $\square$ ihrer Murmeln. $\square$
der Mädchen fand(en) $\square$ ihrer Murmeln. $\square$


## Hearer's task

- Hearer's Task: Buy sweets based on speaker's description 'Some of the girls found all of their marbles and some of the girls found none of their marbles.'

| chocolate | $\square$ | YES | $\square$ | NO |
| :--- | :--- | :--- | :--- | :--- |
| candy | $\square$ | YES | $\square$ | NO |
| gummy bear | $\square$ | YES | $\square$ | NO |

## Methods

## Procedure:

- Participants are randomly assigned to each role (3 times)
- System pairs two participants, pairings change across blocks
- Participants learn reward system with pictures in practice phase


## Items:

- 7 worlds are instantiated by six items
- In one block, a world is shown only once


## Participants:

- 38 German participants (mean age: 29.3, 21 female, 17 male)
- 2 groups with 4 players (8), 5 groups with 2 players (10)
- 6 groups with 3 players plus experimenter (18); experimenter employs critical strategy (produces statements predicted by Benz' model)


## Success rate of utterance

## Calculation of success rate:

- Use average response/interpretation of participants
- data of experimenter are eliminated
- $p_{i}(w \mid u)$ : probability of participant $i$ interpreting utterance $u$ as $w$

$$
\operatorname{Succ}(u \mid w)=\sum_{i \in H(u)} p_{i}(w \mid u) /|H(u)|,
$$

$H(u)$ : set of participants who interpreted utterance $u$.

## Results: Success rate and length of utterance

Results ( $\rightarrow$ : critical strategy):

|  | utterances | world | success \% |
| :--- | :--- | :--- | :--- |
| length |  |  |  |
| $\rightarrow$ (None-any) | $\square_{1}$ | $98 \%$ | 1.0 |
|  | (All-none) |  | $100 \%$ |
| $\rightarrow$ (All-some) | $\square_{2}$ | $94 \%$ | 1.58 |
|  | (All-some but not all) |  | $93 \%$ |
| $\rightarrow$ (All-all) | $\square_{3}$ | $99 \%$ | 1.0 |
| $\rightarrow$ (Some-some, some-none) | $\square_{4}$ | $95 \%$ | 2.72 |
|  | (Some-none, some-some, none-all) |  | $100 \%$ |
|  | (Some-some) |  | $25 \%$ |
| $\rightarrow$ (Some-all, some-none) | $\square_{5}$ | $96 \%$ |  |
| $\rightarrow$ (Some-all, some-some) | $\square_{6}$ | $98 \%$ | 2.63 |
| $\rightarrow$ (Some-all, some-some, some-none) | $\square_{7}$ | $100 \%$ | 2.60 |

## Results: Comparison with individual strategies

- Success rates of individual players with utterances occurring more than once in corpus
- Critical (Benz' model): 0.971, average participant: 0.925
- Critical strategy is significantly better than average participant strategy (one-tailed t test: $\mathrm{p}<.001$ )



## Results: Comparison with individual strategies

- y-axis: 1-Success rates of individual players (utterances occurring more than once).
- x-axis: average length of utterances of strategy
- Critical: av.-length: 1.71429, failure rate: 0.029



## Section 5

## Comparison with other Theories

## Structural Accounts

Sentence level accounts:

|  | Chierchia 2004 | Sauerland 2004 | Observed |
| :--- | :---: | :---: | :---: |
| some some <br>  | $\left\{\square_{4}, \square_{7}\right\}$ | $\left\{\square_{4}\right\}$ | $\square_{4}(25 \%), \square_{2}(75 \%)$ |
| some all | $\left\{\square_{7}\right\}$ | $\left\{\square_{5}, \square_{7}\right\}$ | $\square_{6}(98 \%)$ |
|  <br>  | $\left\{\square_{7}\right\}$ | $\left\{\square_{5}, \square_{7}\right\}$ | $\square_{7}(100 \%)$ |
| some all <br>  <br> some all | $\left\{\square_{5}, \square_{7}\right\}$ | $\left\{\square_{5}, \square_{7}\right\}$ | $\square_{5}(96 \%)$ |

## Predictions of Modern Localism

## Example:

- Conjunction: Some some and some all
- Observed interpretation: $\square_{6}$ (98\%)

Example (Modern Localism: Chierchia et al 2012) possible readings

| some | some and some all | $\square_{3}, \square_{4}, \square_{6}, \square_{7}$ |  |
| :--- | :---: | :--- | :--- |
| some | O[some] | $\ldots$ | $\square_{6}, \square_{7}$ |
| O[some] | some | $\ldots$ | $\square_{5}, \square_{7}$ |
| O[some] | O[some] | $\ldots$ | $\square_{6}, \square_{7}$ |
| O[some | some] | $\ldots$ | $\perp$ |
| O[some | some | $\ldots$ ] | $\square \square_{5}, \square_{7}$ |

## A Bayesian Model

## Take into account:

- Aims at explanatory models (why vs. what)
- Uncertainty about contextual parameters
- Error prone communication
- Fit parametric models to data


## What we tested:

- Pick one specific model: (Qing \& Franke 2014)
- Fitted to experimental data
- Interested in qualitative behaviour


## Reference Game Task

## Speaker:

- chooses object: e.g. green circle
- signals: square, circle, green, blue

Hearer:

- receives signal, e.g. green
- chooses object, e.g. green circle
goal: speaker and hearer choose same object

An experimental token


Frank Goodman (2012), Qing \& Franke (2015), Franke \& Jäger (to appear)

## Possible Parameters Influencing Production

- Probability with which hearer chooses worlds
- Preference for short utterances


## Towards a model: Start with naive interpreter

Probability of choosing world $w$ given utterance $u$ :

$$
P_{\text {literal }}(w \mid u)= \begin{cases}\frac{1}{||u|} & \text { if } w \in u \\ 0 & \text { else }\end{cases}
$$

Expected utility of utterance $u$ given $w$ (disregarding preferences for signals):

$$
E U(u \mid w)=P_{\text {literal }}(w \mid u)
$$

Expected utility of utterance $u$ given $w$ (including preferences for signals):

$$
\left.E U(u \mid w)=P_{\text {literal }}(w \mid u)+\operatorname{cost}(u) . \quad \text { if } w \in u\right)
$$

## Determining Speaker Production Probability

Background: Discrete rational choice theory.

- penalty cost for choosing colour: $0 \geq \operatorname{cost} \geq-1$.
- degree of rationality $\lambda$

$$
\begin{aligned}
P_{\text {prod }}(u \mid w, \lambda, \cos t) & =\frac{\exp (\lambda \cdot E U(u \mid w, \cos t))}{\sum_{u^{\prime}} \exp \left(\lambda \cdot E U\left(u^{\prime} \mid w, \cos t\right)\right)} \\
& =\frac{\exp \left(\lambda \cdot\left(P_{\text {literal }}(w \mid u)+\operatorname{cost}(u)\right)\right)}{\sum_{u^{\prime}} \exp \left(\lambda \cdot\left(P_{\text {literal }}\left(w \mid u^{\prime}\right)+\operatorname{cost}\left(u^{\prime}\right)\right)\right)} \\
P_{\text {inter }}(w \mid u ; \lambda, \cos t) & =\frac{P(w) P_{\text {prod }}(u \mid w, \lambda, \cos t)}{\sum_{w^{\prime}} P\left(w^{\prime}\right) P_{\text {prod }}\left(u \mid w^{\prime}, \lambda, \cos t\right)}
\end{aligned}
$$

## Two Models

## Model 0:

- $\lambda=4.96$, cost $=-0.27$ (Pearson's $\rho: 0.82$ )
- Fitted to average human production strategy
(utterances occurring more than once)
- Literal interpretation strategy
- Fitted: Euclidean distance
- av. length: 1.83201 , success rate: 0.78


## Model 1:

- $\lambda=4.45$, cost $=-0.94$ (Pearson's $\rho: 0.68$ )
- Fitted to average human interpretation strategy
(utterances occurring more than once)
- $\lambda$ and cost represent production strategy against literal interpretation strategy
- Fitted: Euclidean distance
- av. length: 1.10759 , success rate: 0.52806


## Comparison with individual strategies

- y-axis: 1 - Success rates of individual players (utterances occurring more than once).
- X-axis: average length of utterances of strategy
- Critical: av.-length: 1.71429, failure rate: 0.029



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## Conclusion

## Results:

- utterance length increases with complexity of world.
- critical strategy more efficient than average human strategy.
- strategies with higher average utterance lengths not more successful.
- strategies with lower average utterance lengths less successful.
- Results pose problems for structural accounts (localism and globalism)


## Future direction:

- Extend paradigm to more sentence types (downward entailing, disjunction, non-monotonic, and more)
- Look at relation to RSA-models.
- Study scenarios with partial speaker knowledge.


## Thank you for your attention!

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